# Healing Block-assisted Quasi-phase Matching

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# Abstract:

A new QPM structure is proposed to improve the efficiency when the first-order QPM domain length is too short to be fabricated. SHG efficiency 4.69 times higher than the third-order QPM is experimentally demonstrated.

#### I. INTRODUCTION

Engineerable QPM structures have been widely used in many nonlinear optical applications. For example, fanout and multiple QPM devices are useful in wavelengthtunable optical parametric oscillation (OPO) [1,2]. QPM gratings with and without spatially chirped periods are attractive in ultrashort pulse characterizations [3,4]. User-defined phase-matching spectral grids can be realized by several optimization algorithms, such as simulated annealing [5], genetic algorithm [6], and iterative domino [7]. However, the conversion efficiency of a real QPM device could be subject to the minimum domain length  $d_{\min}$  that can be reliably fabricated. In the event of the first-order QPM domain length  $d_1 \le d_{\min}$ , a third-order QPM structure with domain length  $3d_1$  is commonly used while the conversion efficiency is significantly reduced to  $\eta_1/9$  ( $\eta_1$  is the efficiency of the first-order QPM). In this work, we proposed the healing block (HB)-assisted QPM structure to access the efficiency gap for the first time (to the best of our knowledge). It is found that the efficiency of HB-QPM could be higher than  $\eta_1/9$  as long as  $d_{\min} \le 1.54d_1$ . In our experiment, an HB-QPM structure with  $d_{\min}=1.08d_1$ achieved 4.69 times higher SHG efficiency than that of a third-order QPM grating of the same length.

## **II.** THEORY

An HB-QPM structure is composed of repeated substructures; each consists of M regular domains of constant length d plus one longer "healing block" of length  $d_{\text{HB}}$  [Fig. 1(a)]. Under the assumption of plane wave and nondepleted pump, the SHG efficiency of an arbitrary QPM grating is

$$\eta = \eta_{norm} \times \left| G \right|^2, \ G = \frac{1}{L} \int_0^L g(x) e^{i(\Delta k \cdot x)} dx \,, \tag{1}$$

where  $\eta_{norm}$  is the normalized efficiency accounting for the input intensity, crystal nonlinearity, and grating length, *G* is the complex mismatch function value, g(x)denotes the *x*-dependent domain orientation, and  $\Delta k$  is the wavevector mismatch. In HB-QPM, the complex number *G* for a substructure is

$$G_{sub} = G_0 + G_{M+1} + 2\sum_{n=1}^{M} G_n, \ G_n = \frac{e^{i\phi_n}}{\Delta k \cdot L}, \ \phi_n = n\pi + \Delta k \cdot x_n.$$
 (2)

Equation (2) means that the *n*th domain boundary  $x_n$  contributes to *G* by a complex number  $2G_n$  [except for the two end boundaries (n=0, M+1) where the factor of "2" is absent]. For the first *M* regular domains of length  $d=(1+\Delta)d_1$ , we got  $x_n=n(1+\Delta)d_1$ ,  $\phi_n=n\times\delta$ , and the complex numbers  $G_n$ ,  $G_{n-1}$  arising from two adjacent boundaries differ by a constant phase  $\delta=\Delta\times\pi$  [Fig. 1(b)]. Summation of these out-of-phased complex numbers  $\{G_n\}$  would be negligible. By adding a healing block of proper length  $d_{HB}$  to the *M* regular domains such that  $G_{M+1}=G_0$ ,  $G_{sub}$  of every substructure would be identical and can add up constructively [Fig. 1(c), M=1]. The requirement of  $G_{M+1}=G_0$ , i.e.  $\phi_{M+1}=2(M+p+1)\pi$ , results in

$$d_{HB} = (2p+1-M \times \Delta)d_1, \qquad (3)$$

where *p* is the smallest positive integer greater than  $(M+1)\Delta/2$  such that  $d_{HB}>d>d_1$  is satisfied.



Fig. 1. (Color online) (a) Schematic of HB-QPM and the corresponding domain orientation distribution function g(x). (b) The complex numbers  $\{G_n\}$  contributed by regular domains of length  $d=(1+\Delta)d_1$ , where  $\delta=\Delta\times\pi$ . (c) The complex numbers  $\{G_n\}$  and  $G_{sub}$  due to the individual domain boundaries (solid) and the entire substructure (dashed) with M=1.

The SHG efficiency of the HB-QPM normalized to that of the first-order QPM becomes

$$\mu = \left| \frac{G_{sub}}{G_{(1)}} \right|^2 = \left\{ \frac{1}{M + 2p + 1} \times \frac{\sin[(M + 1)\delta/2]}{\sin(\delta/2)} \right\}^2.$$
 (4)

Figure 2(a) shows that the optimal number M (solid) decreases with the increase of regular domain length d, for the phase difference  $\delta$  increases with d and will diminish  $|G_{sub}|$  [Fig. 1(c)]. Once the optimal M is obtained, the corresponding healing block length  $d_{HB}$  (dotted) is determined by Eq. (3). Figure 2(b) illustrates that the SHG efficiency of HB-QPM (solid) is higher than those of the third-order (dashed-dotted) and second-order (dashed, assuming a duty cycle of 0.25) QPM when the regular domain length is shorter than  $1.54d_1$  and  $1.23d_1$ , respectively.



Fig. 2. (Color online) (a) The optimal number of regular domains (solid) and the corresponding normalized healing block length  $d_{\text{HB}}/d_1$  (dotted), as well as (b) the normalized conversion efficiency  $\mu$  (solid) as functions of the normalized regular domain length  $d/d_1$ . The efficiencies due to the second-order (dashed) and third-order (dashed-dotted) QPM are also shown for comparison.



Fig. 3. (Color online) The experimentally measured phase-matching tuning curves of QPM1 (diamonds), QPM2 (circles), and QPM3 (squares), respectively.

#### **III. EXPERIMENT**

We fabricated a 8-mm-long periodically poled MgO doped lithium niobate (PPMgCLN) chip with three different QPM gratings designed for frequency doubling of 1064 nm ( $d_1$ =3.46 µm). The first grating (QPM1) is a third-order QPM with a constant domain length of

 $3d_1$ =10.38 µm. QPM2 and QPM3 are designed by HB-QPM with *M*=3, *d*=4.00µm, *d<sub>HB</sub>*=8.76µm, and *M*=5, *d*=3.75µm, *d<sub>HB</sub>*=8.93µm, respectively. The phase-matching tuning curves were measured by a tunable CW laser and a photodetector. Figure 3 illustrates the experimental results. The peak conversion efficiencies of QPM2 (circles) and QPM3 (squares) are 2.50 and 4.69 times higher than that of QPM1 (diamonds).

## **IV. CONCLUSION**

In summary, we proposed and experimentally demonstrated the HB-QPM structure to enhance the conversion efficiency when the domain length  $d_1$  of the first-order QPM is too short to be reliably fabricated. Our calculation showed that efficiency enhancement over the third-order QPM occurs as long as the regular domain length is shorter than  $1.54d_1$ . In our experiments, the SHG efficiency of HB-QPM could be 4.69 (2.50) times higher than that achieved by the third-order QPM if the regular domain length *d* is 1.08 (1.15) times of  $d_1$ .

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