# Long Range, High accuracy Absolute Distance Measurement by Improved Three-Wavelength Heterodyne Interferometry

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# Abstract

The complexity and non-ambiguity range (NAR) of the conventional three-wavelength heterodyne interferometry are improved by using one phase modulator and a mapping procedure, respectively. Experiments demonstrated 10-mm NAR and an estimated accuracy of 0.65 nm.

# I. INTRODUCTION

Accurate positioning over a long range is essential in many applications, such as semiconductor fabrication. Single-wavelength heterodyne interferometry (1 $\lambda$ HI) can measure absolute distance with precision in the order of nanometers. However, the non-ambiguity range (NAR) is limited by half-wavelength. A larger NAR can be achieved by using multiple (fixed and/or tunable) wavelengths [1-3] at the cost of increased number of optical frequency modulators (OFMs) and/or slower refresh rate if a wavelength tuning system is used [2,3]. In this contribution, we improved the three-wavelength heterodyne interferometer ( $3\lambda$ HI) by using only one OFM (thus simpler lock-in detection), and increased the practical NAR by a new phase point mapping procedure (in place of the conventional multi-step one [2]) that is subject to smaller probability of excessive measurement error. Our experiments demonstrated 10-mm NAR and 0.34-nm accuracy by using three unlocked CW lasers, a common-path geometry for three colors (with interferometric stability), and one electro-optical phase modulator (EOPM).

# II. THEORY

Fig. 1(a) shows the schematic of a conventional polarization-multiplexed  $3\lambda$ HI using three fixed wavelengths [1,2], where three optical frequencies  $v_i$ (i=1,2,3) arranged in the form of Fig. 1(b) are modulated by three acousto-optic modulators (AOMs) with three different frequencies  $f_i (\ll v_i)$ . All the modulated  $(v_i + f_i)$ and unmodulated  $(v_i)$  beams are combined in free space and split into two paths. Three phases  $\phi_1$ ,  $\phi_3$ - $\phi_2$ ,  $\phi_3$ - $\phi_1$  $(\phi_i = 4\pi d/\lambda_i)$  is the phase difference between reference and signal waveforms due to  $v_i$ ) are measured by the superheterodyne scheme [1]. The difference d between the geometric distances of the two interferometer arms is determined by a 3-step estimation procedure (using three manipulated phases  $\Phi^{(1)} \equiv (\phi_3 - \phi_2) - (\phi_3 - \phi_1), \Phi^{(2)} \equiv \phi_3 - \phi_1,$  $\Phi^{(3)} \equiv \phi_1$  to achieve the maximum NAR  $(R_{\text{max}} = 0.5 \times c/\delta v)$ and the minimum measurement error  $\left[\delta_{d,\min}=\delta_{\phi_1}\lambda_1/(4\pi)\right]$ 

where  $\delta_{\phi l}$  means the error of  $\phi_l$ ]. In practice, excessive measurement error (>> $\delta_{d,\min}$ ) occurs for the nonzero phase errors  $\delta_{\phi l,2,3}$  could fail the 3-step estimation procedure occasionally. Assume that the three operation wavelengths are  $\lambda_l$ =1531.997 nm,  $\lambda_2$ =1544.580 nm,  $\lambda_3$ =1557.2807 nm ( $R_{\max}$ =13.3 mm), and  $\delta_{\phi l,2,3}$  are independent normally distributed random variables  $N(0,\sigma_{\phi})$ , simulation shows that the standard deviation  $\sigma_{\phi}$ <0.16° is required to maintain the probability of excessive error  $P_{\varepsilon}$ <1% [Fig. 1(c), open circles].



(Fig. 1. (a) Schematic of conventional  $3\lambda$ HI. AOM#: acousto-optic modulator. (P)BS#: (polarization) beam splitter. PD: photodetector. LP: linear polarizer. QWP#: quarter waveplate. BPF: band-pass filter. PM#: phase meter. (b) The arrangements of the three wavelengths used in  $3\lambda$ HI, respectively. (c) Probability of excessive measurement error  $P_c$  versus the standard deviation  $\sigma_{\phi}$  of normally distributed phase errors  $\delta_{\phi|,2,3}$  for conventional (open circles) and improved (open squares)  $3\lambda$ HI, respectively (assuming  $\lambda_1$ =1531.997 nm,  $\lambda_2$ =1544.580 nm,  $\lambda_3$ =1557.280 nm,  $10^6$  samplings).

We improve the  $3\lambda$ HI in three aspects (Fig. 2). (1) The three AOMs are replaced by one fiber-pigtailed EOPM [4], enabling (a) elimination of the reference arm (for the driving sawtooth wave can serve the reference of the phase meter), (b) a common-path geometry (with interferometric stability) by using a fiber coupler to combine and split chromatic beams. The inherent phase error due to the wavelength-dependent  $V_{\pi}$  of the EOPM is effectively suppressed by a calibration procedure. (2) The three wavelengths  $\lambda_{1,2,3}$  are separated by a grating to measure the three phases  $\phi_{1,2,3}$  simultaneously by a 4channel phasemeter (one for the reference) using one band-pass filter (BPF). In comparison, the conventional geometry needs mixers and three phase meters (with 3 BPFs and 6 channels in total). Consequently, the new architecture is simpler, more economic, and can be easily extended to more operation wavelengths. (3) A direct mapping procedure replaces the 3-step one to get the desired d. Within an NAR, each d corresponds to a unique "phase point"  $(\phi_1, \phi_2, \phi_3)$  and all the phase points

form discrete trajectories (due to the modulo- $2\pi$  limit of  $\phi_i$ ) in the 3D space. In the presence of phase error, the measured phase point  $(\phi'_1, \phi'_2, \phi'_3)$  is projected onto the nearest trajectory to estimate *d*. Simulation shows that a relaxed phase error tolerance ( $\sigma_{\phi} < 0.25^{\circ}$ ) is sufficient to maintain  $P_{\varepsilon} < 1\%$  [Fig. 1(c), squares]. In other words, the phase point mapping procedure permits a larger NAR (smaller  $\delta v$ ) for the same 3 $\lambda$ HI system (with the same phase measurement error  $\sigma_{\phi}$ ).

### III. EXPERIMENT



Fig. 2. Experimental setup. SMF: single mode fiber, PMF: polarization maintaining fiber. PD: photodetector. BS: beam splitter. EOPM: electro-optical phase modulator

Fig. 2 shows our experimental setup. A 3×2 fiber coupler combines light from three independent CW lasers operated at wavelengths  $\lambda_1$ =1531.997 nm (195.63 THz),  $\lambda_2 = 1544.580$  nm (194.04 THz) and  $\lambda_3 = 1557.2807$  nm (192.46 THz), respectively. The combined light is split into two paths, passing through (1) a delay line controlled by a motorized stage with  $\pm 20$ -nm accuracy, and (2) an EOPM driven by a 400-Hz, ±4.75-V sawtooth waveform. The two beams are recombined by a beam splitter (BS), and the three wavelength components are spatially separated by a grating and detected by three InGaAs photodetectors, respectively. The three electric phases  $(\phi'_1, \phi'_2, \phi'_3)$  simultaneously measured by a 4-channel lockin amplifier are processed by a program (in 1 ms) to retrieve the absolute distance. Figure 3(a) shows that the absolute distances d' (dashed) measured by the improved  $3\lambda$ HI differ from the reference distances  $d_r$  obtained by  $1\lambda$ HI (with ~3-nm increments, much less the NAR of  $\lambda_1/2$ ) no more than  $\pm 0.6$  nm (solid) for all the 33,800 sampled distances spanning over 100 µm. There is no excessive error and the standard deviation  $\sigma_d$  of the differences  $\delta_d = d' - d_r$  is 0.19 nm. Since the reference distances  $d_r$  may have some error as well, we estimate the accuracy of d' by the simulation result of Fig. 1(d). In view of the fact that the probability of excessive measurement error  $P_{\varepsilon}$  is less than  $(33,800)^{-1}$ , we estimate the standard deviation of the phase error as  $\sigma_{\phi 1} < 0.153^{\circ}$ . Since the distance error  $\delta_d$  is related to the phase error  $\delta_{\phi 1}$  via a linear relation  $\delta_d = \delta_{\phi 1} \lambda_1 / (4\pi)$ ,  $\delta_d$  is also a normal random variable with standard deviation  $\sigma_d = \sigma_{\phi 1} \lambda_1 / (4\pi) <$ 0.33 nm. The accuracy (95% confidence interval) becomes twice the standard deviation  $2\sigma_d < 0.65$  nm. To confirm the long NAR, we calibrated the stage displacements by recording the interferometric intensity due to  $\lambda_1$  on the fly. The stage stopped for 120 s at each of the 5 positions, during which the absolute distance was measured by  $3\lambda$ HI at a refresh rate of 33 Hz. The resulting values d' are compared with the reference distances d<sub>r</sub> obtained by interferometric fringe counting. As shown in Fig. 3(b), d' and d<sub>r</sub> are in good agreement ( $\sigma_d < 340$  nm) for all the 5 absolute distances spanning over 10 mm. Note that the larger  $\sigma_d$  (compared to the 0.19 nm of the previous test) is dominated by the path length fluctuation within the 120-s data acquisition time due to environmental perturbation, instead of the measurement error.



Fig. 3. (a) Absolute distances measured by  $3\lambda$ HI versus those measured by  $1\lambda$ HI (dashed), and the difference between them (solid). (b) Absolute distances measured by  $3\lambda$ HI versus those measured by interferometric fringe counting (open squares), and the difference between them (open circles). Each error bar means the standard deviation  $\sigma_d$  of the 4,000 discrepancy values.

# **IV. CONCLUSION**

The complexity and NAR of conventional  $3\lambda$ HI are improved by using one (instead of three) phase modulator and a phase point mapping procedure, respectively. The improved geometry can be easily extended to more operating wavelengths (provided by laser comb) such that NAR in the order of meters can be achieved under practical phase error. This work was supported by the National Science Council in Taiwan under grants NSC 100-2221-E-007-093-MY3 and 99-2120-M-007-010.

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