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### Hand gesture recognition using a real-time tracking method and hidden Markov models $\stackrel{\text{\tiny{free}}}{\to}$

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### Abstract

In this paper, we introduce a hand gesture recognition system to recognize continuous gesture before stationary background. The system consists of four modules: a real time hand tracking and extraction, feature extraction, hidden Markov model (HMM) training, and gesture recognition. First, we apply a real-time hand tracking and extraction algorithm to trace the moving hand and extract the hand region, then we use the Fourier descriptor (FD) to characterize spatial features and the motion analysis to characterize the temporal features. We combine the spatial and temporal features of the input image sequence as our feature vector. After having extracted the feature vectors, we apply HMMs to recognize the input gesture. The gesture to be recognized is separately scored against different HMMs. The model with the highest score indicates the corresponding gesture. In the experiments, we have tested our system to recognize 20 different gestures, and the recognizing rate is above 90%.

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Keywords: Hand gesture recognition; Hidden Markov model; Hand tracking

### 1. Introduction

Hand gesture has been one of the most common and natural communication media among human being. Hand gesture recognition research has gained a lot of attentions because of its applications for interactive human-machine interface and virtual environments. Most of the recent works related to hand gesture interface techniques [1] has been categorized as: glove-based method [2,3] and vision-based method. Glove-based gesture interfaces require the user to wear a cumbersome device, and generally carry a load of cables that connect the device to a computer. There are many vision-based techniques, such as model-based [4] and state-based [5] which have been proposed for locating objects and recognizing gesturers. Recently, there have been an increasing number of gesture recognition researches using vision-based methods Table 1.

Huang et al. [6] use 3D neural network method to develop a Taiwanese Sign Language(TSL) recognition system to recognize 15 different gestures. David and Shah 

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[7] propose a model-based approach by using a finite state machine to model four qualitatively distinct phases of a generic gesture. Hand shapes are described by a list of vectors and then matched with the stored vector models. Darrell and Pentland [8] propose space-time gesture recognition method. Signs are represented by using sets of view models, and then are matched to stored gesture patterns using dynamic time warping. 

Starner et al. [9] describe an extensible system which uses one color camera to track hands in real time and interprets American sign language (ASL). They use hidden Markov models (HMMs) to recognize a full sentence and demonstrate the feasibility of recognizing a series of complicated series of gesture. Instead of using instrumented glove, they use vision-based approach to capture the hand shape, orientation and trajectory. The vision-based method selects the 3-D input data as the feature vectors for the HMM input, other HMM-based [10,11] hand gesture recognition systems have also been development. Liang et al. [12] develop a gesture recognition of TSL by using Data-Glove to capture the flexion of 10 finger joints, the roll of palm and other 3-D motion information Table 2. 

Cui and Weng [13] develop a non-HMM-based system which can recognize 28 different gestures in front of 

IMAVIS 1979-29/4/2003-12:22-SHYLAJA-68995-MODEL 5

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F.-S. Chen et al. / Image and Vision Computing xx (0000) xxx-xxx

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119 complex backgrounds. The recognition of this system is 120 93.1% but it relies on a slowly segmentation scheme which 121 takes 58.3 sec for each image. Nishikawa et al. [14] propose 122 a new technique for description and recognition of human 123 gestures. The proposed method is based on the rate of 124 change of gesture motion direction that is estimated using 125 optical flow from monocular motion images.

126 Nagaya et al. [15] propose a method to recognize 127 gestures using an approximate shape of gesture trajec-128 tories in a pattern space defined by the inner-product 129 between patterns on continuous frame images. Heap and 130 Hogg [16] present a method for tracking of a hand using 131 a deformable model, which also works in the presence of 132 complex backgrounds. The deformable model describes 133 one hand posture and certain variations of it and is not 134 aimed at recognizing different postures. Zhu and Yuille 135 [17] develop a statistical framework using principal 136 component analysis and stochastic shape grammars to 137 represent and recognize the shapes of animated objects. It 138 is called flexible object recognition and modeling system 139 (FORMS). Lockton et al. [18] propose a real-time gesture 140 recognition system which can recognize 46 ASL letter 141 spelling alphabet and digits. The gestures that are 142 recognized by [18] are 'static gestures' of which the 143 hand gestures do not move.

144 Different from [18], this paper introduces a hand gesture 145 recognition system to recognize 'dynamic gesture' of which 146 a gesture in performed singly in complex background. 147 Different from previous HMM-based gesture recognition 148 systems, our system do not use instrumented glove, nor any 149 markers, but use 2D video input. Our system tracks the 150 moving hand and analyzes the hand-shape variation and 151 motion information as the input to the HMM-based 152 recognition system. The system consists of three modules: 153 a real-time hand tracking, feature extraction, HMM training, 154 and HMM-based gesture recognition. First, we introduce a 155 real time hand gesture tracking technique which can track 156 the moving hand and then extract the hand shape from 157 complex background. It is a simple and reliable method 158 developed as a real-time image processing subsystem which 159

161	Table 2
162	The recognition rate of one-hand gesture

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Table 2

Two Methods	Training data (%) (1200 sequences)	Testing data (%) (1200 sequences)
FD only	97	90.5
FD and motion	98.5	93.5

consists of five basic complementary image processes: motion detection, skin color extraction, edge detection, movement justification, and background subtraction.

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178 We apply the FD to characterize the spatial information and the optical flow method for motion analysis to 179 180 characterize the temporal information. We combine FD 181 and motion information of the input image sequence as our 182 feature vector. With these extracted feature vectors, we can 183 train our system using HMM approach which is used to 184 recognize the input gesture. In training phase, we apply 185 HMM to describe the gestures in term of model parameters 186 for each different gesture. The gesture to be recognized in 187 separately scored against different HMMs. The model with 188 the highest score is selected as the recognized gesture. Our 189 system consists of 20 different HMMs which are used to test 190 20 different hand gestures. The experimental results show 191 that the average recognition rate is above 90%. 192

Fig. 1 shows the flow diagram of our hand gesture recognition system consisting of three phases: the feature extraction phase, the training phase, and the recognition



IMAVIS 1979-29/4/2003-12:22-SHYLAJA-68995- MODEL 5

#### F.-S. Chen et al. / Image and Vision Computing xx (0000) xxx-xxx



Fig. 2. (a) The origin frame, (b) apply our threshold, (c) apply Ostu thresholding.

phase. We combine FD and motion features as the feature vector to describe the moving object. Each feature vector is represented by a symbol. Each symbol corresponds to the designated partition generated through the vector quantiza-tion of the feature vectors of all possible hand-shapes of the training gestures. For each feature vector, a symbol is assigned. In our system, we represent the input image sequence by a sequence of symbols. In training phase, we need to build a HMM for each gesture. In the recognition phase, a given input gesture is tested by every HMM with different model parameters. The outcome of the HMM with the maximum likelihood function is identified to recognize the gesture. 

### 2. Hand tracking and handshape extraction

Here, we develop a real-time hand tracking method which is robust and reliable in complex background. To track the moving hand and then extract the hand shape fast and accurately, we need to consider the trade-off between the computation complexity and robustness.

#### 2.1. Feature extraction

In our system, the motion of the object provides important and useful information for object localization and extraction. To find the movement information, we assume that the input gesture is non-stationary. When objects move in the spatial-time space (an image sequence),



$$D_i(x, y) = T_i\{|F_i(x, y) - F_{i+1}(x, y)|\}$$
(1)

where  $T_i$  is a thresholding function,  $F_i(x, y)$  and  $D_i(x, y)$  are all 160 × 120 images, and  $D_i(x, y)$  is binary image defined as follows

$$D_i(x,y) = \begin{cases} 1, & |F_i(x,y) - F_{i+1}(x,y)| \ge \text{threshold} \\ 0, & \text{otherwise.} \end{cases}$$
(2)

(1) Thresholding. Having extracted the moving object region, we can apply the thresholding on the frame difference (i.e. Eq. (2)) to extract the possible moving region in complex background. We find that conventional thresholding methods, such as Ostu thresholding [27], are not suitable for the case of detecting motion difference. Instead, we use a simple thresholding technique to extract moving regions. The threshold for motion detection is determined as  $t_{\rm M} = 0.2\mu$ , where  $\mu$  is the average luminous of captured image  $F_i(x, y)$ . Fig. 2 shows that if there is no significant movement, Ostu thresholding method will generate a lot of noise. We choose the weighting factor 0.2 because we do not need highly precise segmented image. Our thresholding technique is not very sensitive to the speed of the hand movement, so that our method more stable than the Ostu method. 



279Fig. 3. (a) The origin frame, (b) extracted skin regions satisfying R > G > B, and (c) compare the colors of the extracted skin regions with the sample skin335280color.336

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F.-S. Chen et al. / Image and Vision Computing xx (0000) xxx-xxx



Fig. 4. (a) The origin frame, (b) the edge detection result.

(2) Skin color detection. Skin can be easily detected by using the color information. First, we use the constraint, i.e. R > G > B, to find the skin color regions which may include a wide range of colors, such as red, pink, brown, and orange color. Therefore, we will find many regions other than the skin regions. However, those non-skin regions satisfy our constraint will be excluded due to there is no motion information, e.g. a region in orange color will not be misidentified as the hand region. Second, we may obtain some sample colors from the hand region. To find the skin regions, we compare the colors in the regions with the prestored sample color. If they are similar, then the region must be skin region. The hand region is obtained by the hand tracking process in the previous frame. Fig. 3 shows our skin detection results. The rectangular region is the hand region in the previous frame. Finally, we may eliminate some skinsimilar colors, e.g. the orange color, and denote the skin color image as  $S_i(x, y)$ .

(3) Edge detection. Edge detection is applied to separate the arm region from the hand region. It is easy to find that there are fewer edges on the arm region than on the palm



region  $D_i S(x, y)$ , (c) skin color region  $S_i(x, y)$ , (d) edge region  $E_i(x, y)$ . 392



Fig. 6. The combined region  $C_i(x, y)$ .

region. Here, we use a simple edge detection technique (e.g. Kirsch edge operator) to obtain different direction edges, and then choose the absolute maximum value of each pixel to form the edge image of *i*th frame as  $E_i(x, y)$ . Fig. 4 shows that the edges on the arm region are less than those on the palm region. We combine edge, motion, skin color region information to allocate the hand region.

(4) Combination of motion, skin color, and edge. The hand gestures information consists of movement, skin color and edge feature. We use the logic 'AND' to combine these three types of information, that is

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$$C_i(x, y) = D_i(x, y) \land S_i(x, y) \land E_i(x, y)$$
(3)

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where  $D_i(x, y)$ ,  $S_i(x, y)$  and  $E_i(x, y)$  indicate the movement, skin color and edge images. The combined image  $C_i(x, y)$  as many features that can be extracted. Because the different image processing methods have extracted different kind of information. Each image consists of different characteristic regions such as motion regions, skin color regions and edge regions as shown in Fig. 5. Fig. 6 shows the combined region  $C_i(x, y)$ . The combined image consists of a large region in the palm area and some small regions in the arm area. We may separate these two regions to allocate the hand region.

(5) Region identification. A simple method for region identification is to label each region with a unique integer number which is called the labeling process. After labeling, the largest integer label indicates the number of regions in the image. After the labeling process, the small regions can be treated as noise and then be removed. Fig. 7(a) shows that the labeling results and Fig. 7(b) shows the center position  $p_{c}(i)$  of the hand region. We use  $L_{i}(x, y)$  to indicate the largest labeled region in Frame *i*.



Fig. 7. (a) The labeling results  $L_i(x, y)$ , (b) the correct center position.

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Fig. 8. The flow diagram of hand gesture tracking system.

### 2.2. Robustness and low complexity

Using motion and color information is not sufficient, and hand-shape is not always the largest labeled region. If there are other skin-color objects moving rapidly, the tracking process may fail. We need to take advantage of the motion smoothness constraint for trajectory justification, then use background subtraction to find the foreground object, and finally identify the hand region.

### 2.2.1. Hand gesture trajectory justification

Based on the assumption that the hand object move smoothly between two connected frames, we develop a trajectory justification algorithm. We assume that the movement of the hand is in a constant speed. For current frame  $F_i$ , we get the center point  $p_C(i)$  of the extracted hand region. We assume smooth trajectory so that the variation of  $p_C(i)$  is constrained in a certain range. If the variation of  $p_C(i)$  is out of a certain range (i.e.  $|p_C(i) - p_R(i-1)| > \delta$ ), we increase the wrong (or bumpy) position counter, i.e. WC = WC + 1, else we set  $p_R(i) = p_C(i)$ . To avoid the trajectory of  $p_C(i)$  being bumpy for while, we check if WC > 3. If it is not, then the hand gesture is suppose to be at a right position, and we may set  $p_R(i) = p_R(i-1)$ . If WC > 3, then the hand gesture may be identified at a wrong position, therefore, we change the right position  $p_R(i) =$  $p_C(i)$ , reset WC = 0, and go to next frame  $F_{i+1}$ . 

### 2.2.2. Processing ROI

Fig. 8 shows the flow diagram of our hand gesture tracking system. In previous section, we have mentioned how to generate five image frames:  $D_i(x, y)$ ,  $S_i(x, y)$ ,  $E_i(x, y)$ ,  $C_i(x, y)$  and  $L_i(x, y)$ . The three function blocks indicate motion detection, edge detection, skin color detection, which can operate in parallel. To reduce the computation complexity, we do not process the entire image frame but concentrate on the region of interest (ROI). For instance, one ROI is a part of  $F_i(x, y)$ , where the corresponding  $D_i(x, y) \neq 0$ . We deal with the first ROI to obtain  $S_i(x, y)$ . The other ROI is also part of the  $F_i(x, y)$ , where the corresponding  $S_i(x, y) \neq 0$ . Similarly, we process the second ROI to obtain  $E_i(x, y)$ . Fig. 9 shows the step-by-step processing of motion detection, skin color detection, and edge detection. We can dramatically reduce the computation complexity of our system. 

### 2.2.3. Background subtraction

For gesture recognition process, we need more hand gesture information. We use a simple background subtraction technique to obtain the hand gesture shape. We create the background model  $BG_i$  by using the first frame  $F_1(x, y)$ . Fig. 10 shows the foreground region, and Fig. 11 shows the procedure to obtain the foreground.

To update our background model, we adapt our back-ground model by using current frame  $F_i$  and foreground region  $FG_i$ . We have generated two different types of foreground regions, one is  $FG1_i = FG_i$ , which is used to obtain the hand gesture region; and the other is  $FG2_i$ ,  $(FG2_i)$ is obtained by dilating  $FG1_i$ ), which is applied for background updating process.  $FG1_i$  has a compact shape, so that it can be used to obtain the hand region. Because there are small errors on the boundary of foreground and background, we do not use  $FG1_i$  to update the background. 



Fig. 9. The three function blocks: (a) motion detection, (b) skin color detection, (c) edge detection.



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Fig. 11. Background subtraction process.

We generate  $FG2_i$  for background updating. We only update the background region where  $FG2_i \neq 0$ . Fig. 12 shows the difference of these foreground regions. The background update equation is

$$BG_{i+1} = (1 - w)BG_i + wF_i$$
(4)

We update background gradually, and the weighting factor *w* is 0.1. The updating process is more reliable for a smaller *w*. Finally, we have the foreground region which does not really indicate the human hand. We need to apply the skin color analysis and the hand region position tracking to correctly extract the hand region. Fig. 13 shows the results of hand gesture region extraction process. 623

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### 2.2.4. Local tracking of the hand gesture region

To find a more precise hand region, we use the 626 foreground region information. The hand position has 627 been found by using motion, skin color and edge 628 information. Sometime, the identified locations will not at 629 the center of the real hand region. This is because the 630 extracted information are located on the boundary of the 631 moving object. Therefore, the local refinement is necessary. 632 The overall system for hand region tracking has two stages: 633 the first stage is focus on the motion information, whereas 634 the second stage is focus on the foreground information. The 635 local tracking processing is mentioned as follows: (a) select 636 the foreground and skin color region near the inaccurate 637 center; (b) select the boundary points in the foreground 638 region; and (c) find the center of the boundary points as a 639 new center. We may formulate the process as 640

$$p_{C2}(i) = T_{C} \{ T_{R}(p_{C}(i), FG_{i} \land E_{i} \land S_{i}) \}$$
(5) 
$$\begin{array}{c} 641 \\ 642 \\ 642 \end{array}$$

Where  $p_{C2}(i)$  is the new center at the second stage.  $T_{C}\{\bullet\}$  is a center finding operator, and  $T_{R}(A, B)$  is an operator to find a region in *B* that is near the point *A*. Fig. 14 shows the difference between those two stages.

After refining the hand gesture center point, we may find the bounding box of hand region. We find the bounding box by using the foreground, the skin color information, and the center point located in the second stage. We search the boundary of hand region from center to top, bottom, left, and right. We use four parameters to describe the width and the height of the extracted hand region, e.g. LW,RW,TH, and BH shown in Fig. 15(a).

Since the arm region is not the target region, we develop a simple criterion to obtain a more precise hand region. The bounding box is determined by the following criteria: (1) If RW > LW then RW = 1.1LW else LW = 1.1RW; and (2) If TH > BH then TH = 1.1BH else BH = 1.1TH. In the Fig. 15(a), the length TH is shorter than BH, we let BH = 1.1TH, and similarly RW = 1.1LW. Fig. 15(b)





IMAVIS 1979-29/4/2003-12:23-SHYLAJA-68995- MODEL 5

F.-S. Chen et al. / Image and Vision Computing xx (0000) xxx-xxx

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Here, we illustrate some experimental results of the hand 691 tracking process. The tracked hand-shape includes different 692 types of gestures and the gestures made by different persons. 693 We assume no camera panning nor zooming, and there is 694 only one hand needs to be tracked. We allow the other 695 moving objects in the background, but there is only one 696 moving hand in the foreground. For each frame of the video 697 sequence, the bounding box tracked automatically is 698 compared to a bounding box selected manually to measure 699 the error in width w and height h. There are two 700 performance measurements; one is the gesture location 701 missed percentage 702

$$e_{\rm m} = \frac{\rm number of times the centers are not located}{\rm total frame number}$$
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The other is the normalize error in bounding box size defined as below

$$e_{w}(i) = 1 - \frac{w(i)}{w_{a}(i)}$$
 and  $e_{h}(i) = 1 - \frac{h(i)}{h_{a}(i)}$  (7)

where w(i) and h(i) are the correct dimensions of the bounding box of *i*th frame selected manually, and  $w_a(i) = LW(i) + RW(i), h_a(i) = TH(i) + BH(i)$  are the dimensions of the bounding box of *i*th frame selected by our system. The image size is  $160 \times 120$ . Fig. 16 shows some input image sequences and the extracted



Fig. 14. Difference between the first stage center and the local tracking
center. The solid line is the trajectory of the first stage center, and dotted
line is the trajectory of the second stage center.

#### 3. Feature selection for object description

748 Features are obtained from the input image sequence of 749 hand gestures, they are further converted to symbols which 750 are the basic elements of the HMM. Effective and accurate 751 feature vectors play a crucial role in model generation of the 752 HMM. For selecting good features, the following criteria are 753 considered useful: (1) Features should be preferably 754 independent on rotation, translation and scaling. (2) 755 Features should be easily computable. (3) Features should 756 be chosen so that they do not replicate each other. This 757 criterion ensures efficient utilization of information content 758 of the feature vector. The features obtainable from the image 759



Fig. 15. (a) Four parameter of hand gesture bounding box, (b) new hand 783 gesture bounding box. 784

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F.-S. Chen et al. / Image and Vision Computing xx (0000) xxx-xxx

Fig. 16. Some image sequence in our database and processing result.

sequence of hand gesture are spatial and temporal features.
To extract the shape features, we choose the FD to describe
the hand shape, and to extract the temporal features, we use
motion analysis to obtain the non-rigid motion characteristics of the gesture. These features should be invariant to
the small hand shape and trajectory variations and it is also
to lerant to small different gesture-speed.

### 830 3.1. Fourier descriptor

We may describe the objects by their features in the frequency domain, rather than those in the spatial domain. The local feature property of the node is represented by its Fourier Descriptors (FD) [19,20]. Assume the hand-shape is described by external boundary points,  $\{x(m), y(m)\}$ , then we may use the FD representation for boundary description. To extract the external boundary points of a hand shape, we may use the contour following algorithm. To represent the boundary points, we may find the Fourier series of x(m) and 

y(m), which are defined as a(n) and b(n). For a closed boundary, this representation is called FD. The elements of the vector are derived as S(n) = r(n)/r(1) where, r(n) = $[(a(n))^2 + (b(n))^2]^{1/2}$ , n = 1, 2, ... Using of FD vectors of dimension 10 for hand written digit recognition is sufficient [20]. Here we assume that the local variation of hand-shape is smooth so that the high order terms of its FD are not necessary, so using 22 harmonics of the FD's is enough to describe the macroscopic information of the hand figures. 

The advantage of using the FD is due to its size-invariant properties. For different scaled objects, only the magnitudes of their FD coefficients are changed by the same factor. Furthermore, from Fig. 18, we may find that rotating the object only causes a phase change. The magnitude S(n) is independent of the phase, and it is unaffected by rotation. If the magnitude of the FD coefficients is normalized, the FD representation is invariant to object size. Finally, we consider the effect of noise and quantization errors on the boundary. This will cause local variation of high frequency, 





Fig. 17. The percentage error in bounding box size and location loss rate.

and it will not change to low frequencies. Hence, if the high frequency components of the spectrum are ignored, the rest of the spectrum is unaffected by noise.

### 3.2. Motion analysis

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In the image sequence of hand gesture, there are local 917 motion and global motion. The global motion is the 918 translation of the hand and the local motion is non-rigid 919 motion of the fingers or rotation of the hands. Therefore, we 920 need to estimate the entire motion field of the two 921 consecutive image frames. The motion estimation is based 922 on the space-temporal image intensity gradients called the 923 optical flow Equation [21]. The optical flow equation is 924 developed in conjunction with an appropriate space-925 temporal smoothness constraint, which requires that the 926 neighboring displacement vectors very smooth. The magni-927 tude and phase of the motion vector field indicates the speed 928

distribution of the magnitude and phase of the motion vector 953 field are extracted as the motion features. 954

Here, we partition the magnitude distribution of the 955 motion vectors into ten intervals. Let  $P_{e}(i)$  denote the 956 number of motion vectors belonging to magnitude interval i, 957 then we have  $f_e(i) = P_e(i)/$  (total pixels of a frame), where 958  $1 \le i \le 10$  and  $f_e(i)$  denotes the features extracted from the 959 magnitude of the motion vector. We also partition the phase 960 distribution of the motion vector field into 8 intervals. Let 961  $P_{\rm p}(i)$  denote the number motion vectors belong direction 962 interval I, we have  $f_p(i) = P_p(i)/(\text{total pixels of a frame})$ , 963 where  $1 \le i \le 8$  and  $f_p(i)$  denote the features extracted 964 from the direction of the motion vector. 965

From motion analyzing of two consecutive image 966 frames, we find that the motion vectors are pointing in 967 different directions. The motion of different fingers creates 968 the motion vectors in various directions. From the phase 969 histogram, we find that the peaks of some intervals represent 970 the major directions of different local motions. From the 971 magnitude histogram, we can also find the only peak of the 972 first interval that indicates the global motion (see Fig. 19). 973

Besides the above analysis of the motion direction and 974 magnitude distribution, we can find other features related to 975 the distribution of the motion vector field. We can assume 976 that the motion vector field is an intensity of motion in 2D 977 space  $X = \{(x, y)\}$ . We apply the vector field v(x, y, t) to 978 characterize the motion distribution. A suitable feature for 979 the characterization of the motion distribution at time 980 instance t is the center of gravity  $\vec{m}(t)^T = [mx(t), my(t)]$  as 981

$$mx(t) = \frac{\sum_{x,y} x.v(x, y, t)}{\sum_{x,y} v(x, y, t)} \qquad my(t) = \frac{\sum_{x,y} y.v(x, y, t)}{\sum_{x,y} v(x, y, t)}$$
(8)

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F.-S. Chen et al. / Image and Vision Computing xx (0000) xxx-xxx





1026 The vector  $\vec{m}(t)$  can also be interpreted as the 'center of 1027 motion' of the image. v(x, y, t) denotes the magnitude of the 1028 motion vector at position (x, y) at time t. To increase 1029 the modeling capacity of the HMMs for the movements of 1030 the center, we include the delta features  $\Delta \vec{m}(t)$  of  $\vec{m}(t)$  for the 1031 'center of motion' into the feature vector. The delta features 1032 are defined as  $\Delta mx(t) = mx(t) - mx(t-1)$  and  $\Delta my(t) =$ 1033 my(t) - my(t-1). Another useful feature is the average 1034 absolute deviation of the motion in all points of the images 1035 from the center of motion  $\sigma x(t)^T = [\sigma x(t), \sigma y(t)]$ , which is 1036 defined as 1037

This feature is very similar to the second translation 1046 invariant moment of the distribution, but it is more robust 1047 against noise in the image sequence. It can also be 1048 considered as 'wideness of the movement'. In motion 1049 analysis, we have created 24 features, they are 10 motion 1050 magnitude features, 8 motion direction features, 1051  $m_x, m_y, \Delta m_x, \Delta m_y, \sigma_x$ , and  $\sigma_y$ . 1052

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#### 4. Gesture recognition using HMMs 1055

1056 HMMs have been widely and successfully used in speech 1057 recognition and handwriting recognition [22]. Conse-1058 quently, they seem to be effective for visual recognition of 1059 complex, structured hand gestures such as sign language 1060 1061 recognition [23,24]. A HMM can be employed to represent the statistical behavior of an observable symbol sequence in 1062 terms of a network of states. For each observable symbol, it 1063 can be modeled as one of the states of the HMM, and then 1064

1082 the HMM either stays in the same state or moves to another state based on a set of state transition probability associated 1084 with the state. The variety of the observable symbols for which the HMM uses a particular state is described in terms of the distribution of probability that each observable symbol will occur from that state. Thus, an HMM is a doubly (observable and hidden) stochastic model where the observable symbol probability distribution for each state 1090 captures the intra-state variability of the observable symbols, and the state transition probability describe the underling dynamic structure of the observable symbols.

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1093 We use HMMs to recognize different gestures because of 1094 their simplicity and reliability. The HMM uses only three 1095 parameters: the initial state probability vector, the state-1096 transition probability matrix, and the observable symbol 1097 probability matrix. Analysis of dynamic images naturally 1098 will yield more accurate recognition than that of a single 1099 static image. Gestures are recognized in the context of entire 1100 image sequences of non-constant lengths. Using an HMM 1101 for gesture recognition is advantageous because it is 1102 analogous to human performance which is a doubly 1103 stochastic process, involving a hidden immeasurable 1104 human mental state and a measurable, observable human 1105 action. 1106

#### 4.1. Vector quantization for symbol generation

To model various gesture expressions, we train different 1110 HMMs to model different hand gestures. First, we must 1111 convert multi-dimensional vector sequences to one-dimen-1112 sional symbol sequences. The preprocessing algorithm is 1113 the vector quantization (VQ) [25,26]. In an HMM-based 1114 approach, we need to quantize each multi-dimensional 1115 feature vector sequence into a finite symbol sequence for 1116 HMMs. The purpose of designing an M-level VO (called a 1117 codebook with size M) is to partition all k-dimensional 1118 training feature vectors into M clusters, whose centroid is 1119 the k-dimensional vector  $c^i$ , with a quantized value named 1120

codeword (symbol)  $o^i$ . VQ will cause a quantization error 1121 between each training feature vector x and  $c^{i}$ . As the size of 1122 the codebook increases, the quantization error decreases, 1123 1124 however, the required storage for the codebook entries increases. There is a trade-off to define the size of the 1125 codebook. 1126

To have a good recognition performance in using 1127 HMMs, we design a codebook for vector quantizing each 1128 k-dimensional training feature vector x into a symbol  $o^i$  with 1129 1130 minimum quantization error. According to our experimental 1131 result, the recognition system has high performance when 1132 the size M = 64 of the codebook. This VQ algorithm uses 1133 iterative method, splits the training vectors from assuming 1134 whole data to be one cluster to  $2, 4, 8, ..., M(M = 2^n)$ 1135 clusters, and determines the centroid for each cluster. The 1136 centroid of each cluster is refined iteratively by k-means 1137 clustering. Once the final codebook is obtained, it is used to 1138 quantize each training and testing feature vector into a 1139 symbol. A symbol is assigned to each partition of the k-1140 dimensional VQ space. The symbol generation process is 1141 illustrated in Fig. 20. 1142

#### 1143 4.2. Hidden Markov models 1144

1145 In the Markov model, the state sequence is observable. 1146 The output observable event in any given state is 1147 deterministic, not random. This will be too constraining 1148 when we use it to model the stochastic nature of the human 1149 performance, which is related to doubly stochastic pro-1150 cesses, namely human mental states (hidden) and human 1151 actions (observable). It is necessary that the observable 1152 event is a probabilistic function of the state. HMM is a 1153 representation of a Markov process and is a doubly 1154 embedded stochastic process with an underlying stochastic 1155 process that cannot be directly observed, but can only be 1156 observed through another set of stochastic processes that 1157 produce the sequence of observable symbols. 1158



Fig. 20. Preprocessing of the hand gesture recognition system.

We define the elements of an HMM as follows. N is the 1177 number of states in the model. The state of the model at time 1178 t is  $q_t, 1 \leq q_t \leq N$  and  $1 \leq t \leq T$  where T is the length of the 1179 output observable symbol sequence. M is the size of the 1180 codebook or the number of distinct observable symbols per 1181 state. Assume  $o_t$  is one of all possible observable symbols for 1182 each state at time t, then  $0 \le o_t \le M - 1 \pi_N$  is an N-1183 element vector indicates the initial state probability.  $\pi_N =$ 1184  $\{\pi_i\}$ , where  $\pi_i = P(q_i = i), 1 \leq i \leq N$ .  $A_{N \times N}$  is an  $N \times N$ 1185 matrix specifying the state-transition probability that the 1186 state will transit from state *i* to state *j*.  $A_{N \times N} = \{a_{ii}\}$  where  $\times$ 1187  $a_{ij} = P(q_t = j | q_{t-1} = i), 1 \le i, j \le N \text{ and } a \ge 0, \sum_{j=1}^N X$ 1188  $a_{ij} = 1. B_{M \times N}$  is an  $M \times N$  matrix specifying that the system 1189 will generate the observable symbol  $o_t$  at state j and at time t. 1190  $B_{M \times N} = \{b_i(o_t)\}$  where  $b_i(o_t) = P(O_t = o_t | q_t = j), 1 \le i \le j$ 1191  $N, 0 \le o_t \le M - 1, b_j(o_i) \ge 0$ , and  $\sum_{o_t=0}^{M-1} b_j(o_t) = 1$ . 1192

The complete parameter set  $\lambda$  of the discrete HMM is 1193 represented by one vector  $\pi$  and two matrices A and B. To 1194 accurately describe a real-world process such as gesture 1195 with an HMM, we need to appropriately select the HMM 1196 parameters. The parameter selection process is called the 1197 HMM 'training.' This parameter set  $\lambda$  can be used to 1198 evaluate the probability  $P(O|\lambda)$ , that is to measure the 1199 maximum likelihood performance of an output observable 1200 symbol sequence O, where T is the number of frames for 1201 each image sequence. For evaluating each  $P(O|\lambda)$ , we need 1202 to select the number of states N, the number of observable 1203 symbols M (the size of codebook), and then compute the 1204 results of probability density vector  $\pi$  and matrices A and B 1205 by training each HMM from a set of corresponding training 1206 data after VQ. 1207

There are three basic problems in HMM design: (1) 1208 Probability evaluation: How do we efficiently evaluate 1209  $P(O|\lambda)$ , the probability (or likelihood) of an output 1210 observable symbol sequence O given an HMM parameter 1211 set  $\lambda$ . (2) Optimal state sequence. How do we determine an 1212 optimal state sequence  $q = \{q_1, q_2, ..., q_T\}$ , which is associ-1213 ated with the given output observable symbol sequence O, 1214 by given an HMM parameter set  $\lambda$ . (3) Parameter 1215 Estimation. How do we regulate an HMM parameter set  $\lambda$ 1216 to maximize the output probability  $P(O|\lambda)$  of generating the 1217 output observable symbol sequence. 1218

(1) Probability evaluation using the forward-backward 1219 *procedure*. We compute the output probability  $P(O|\lambda)$  with 1220 which the HMM will generate an output observable symbol 1221 sequence  $O = \{o_1, o_2, \dots, o_T\}$  given the parameter set  $\lambda =$ 1222  $(\pi, A, B)$ . The most straightforward way to compute this is 1223 by enumerating every possible state sequence of length T, 1224 so there will be  $N^T$  possible combinations of state sequence 1225 where N is the total number of states. Suppose there is one 1226 state sequence  $q = \{q_1, q_2, \dots, q_T\}$ . Fortunately, we can use a 1227 more efficient procedure called the Forward-Backward 1228 procedure [29] to overcome this limitation. 1229

(2) Optimal state sequence using the viterbi algorithm. 1230 We use a dynamic programming method called the 1231 Viterbi algorithm [28] to find the single best state sequence 1232

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1233 q = (q1, q2, ..., qT) (or the most likely path) given the 1234 observable symbol sequence  $O = (o_1, o_2, ..., o_T)$  and the 1235 HMM parameter set  $\lambda$  in order to maximize  $P(q|O, \lambda)$ . Since

$$\begin{array}{l} 1236\\ 1237\\ 1238 \end{array} P(q|O,\lambda) = \frac{P(q,O|\lambda)}{P(O|\lambda)} \end{array}$$
(10)

<sup>1239</sup> <sup>1240</sup> Maximizing  $P(q|O, \lambda)$  is equivalent to maximizing <sup>1241</sup>  $P(q, O|\lambda)$  using the Viterbi algorithm.

(3) Parameter estimation using the baum-welch method. 1242 We can use a set of training observable symbol sequences to 1243 adjust the model parameters in order to build a signal model 1244 that can be used to identify or recognize other sequences of 1245 observable symbols. There is, however, no efficient way to 1246 optimize the model parameter set that globally maximizes 1247 the probability of the symbol sequence. Therefore, the 1248 Baum-Welch method [29] is used to choose the maximum 1249 likelihood model parameter set  $\lambda = (\pi, A, B)$  such that its 1250 likelihood function  $P(O|\lambda)$  is locally maximized using an 1251 iterative procedure. 1252

### 1254 1255 **5. Experimental results**

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In the experiments, the subject, who uses a single hand to 1257 make hand gesture, is standing before any stationary 1258 background with normal lighting. The proposed real-time 1259 tracking system can track and identify the moving objects in 1260 front of a stationary background. We may allow some small 1261 objects moving in the background which will not be 1262 extracted and mistreated as a moving hand. We have tested 1263 twenty different hand gestures selected from TSL. Each 1264 hand gesture consists of a sequence of image frames 1265 capturing a single hand moving in different directions with 1266 constant or time-varying hand shape. 1267

Each hand gesture is performed 3 times by 20 different 1289 individuals. There are 60 different image sequences 1290 captured for each hand gesture. There are twenty different 1291 gestures, and 1200 image sequences are used for training. 1292 The size of each gray-level image frame is  $256 \times 256$ , its 1293 frame rate is 30 frames/sec, and each gesture-making takes 1294 about one second. The input image sequence is divided into 1295 three different time intervals: in the first (begin) period, the 1296 sign language speaker remains silent (no gesture), then in 1297 1298 the second (action) period, the speaker starts making one 1299 simple hand gesture, and finally, in the last (end) period, the 1300 speaker remains silent again.

1301 In the experiments, six gestures have constant hand 1302 shape, whereas fourteen gestures have time-varying hand 1303 shape. They may have similar or different moving 1304 trajectories. The simply single hand gestures can be 1305 completed in less than one second. The host computer was 1306 equipped with a Pentium IV 1.2 GHz CPU and 128 MB 1307 main memory. In the experiments, the hand tracking and the 1308 handshape extraction are operating in real-time. The 1309 following feature extraction processes includes FD and 1310 motion analysis may finish in less than one second. Totally, 1311 the recognition system about one second from image 1312 sequence capturing to gesture recognizing. In the training 1313 stage, for each gesture, we have asked 20 different 1314 individuals to make the gestures three times, and for each 1315 gesture, we have 60 different training image sequences to 1316 generate the corresponding HMM. 1317

Each input image sequence is pre-processed by hand region extraction process for contour information and coding. 1200 image sequences are used in training phase, and 1200 image sequences are used in testing phase. Our system consists of two methods: (1) using only contour information and (2) using combined contour information

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F.-S. Chen et al. / Image and Vision Computing xx (0000) xxx-xxx

345	Table 3
346	The error rate of the gesture recognition system using FD and motion vector
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1347	Gesture	01	02	03	04	05	06	07	08	09	10	11	12	13	14	15	16	17	18	19	20
1348	Error (%)	7	1	0	11	12	5	4	7	11	6	5	11	3	0	10	4	13	15	0	3
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and motion information. The extracted information is 1351 converted to vector sequences and then quantized into 1352 symbol sequences for both of the training and recognition 1353 processes. 1354

The same gesture made by different individuals may 1355 looks different because of different hand-shapes and gesture 1356 speed. To design a robust recognition system, the training 1357 data are selected to cover all possible hand-shapes for each 1358 individual. Before using HMMs for training or recognition 1359 1360 process, any vector sequence is preprocessed by VQ to an observable symbol sequence O. The codebooks are created 1361 based on their corresponding training data. The codebook 1362 size M, which is power of 2, is chosen by experiments. We 1363 have tried different codebook sizes, and find that M = 64 is 1364 the best choose because the recognition rate does not have 1365 1366 any significant improvement for M > 64. Based on these training symbol sequences, we can effectively generate the 1367 1st-order 4-state HMM for modeling the gesture. We have 1368 tested our system by using three different state number 1369 HMMs (3-state, 4-state and 5-state), and we found that the 1370 4-state HMM has proved to generate the best performance. 1371 (1) Fourier descriptor (FD) only. Totally 1200 image 1372 sequences are collected for 20 different gestures, thus each 1373 kind of gesture with 60 sequences in average, in training 1374 phase and other 1200 sequences are collected for test. The 1375 recognition rate of using training data for testing is 97%, and 1376 the recognition rate of using testing data is 90.5%. The error 1377 rates of recognizing gesture 9, 12, 17 and 18 are among the 1378 highest. This is because the extracted hand shape may be not 1379

precise and the hand-shapes of these gestures are similar to 1380 1381 one another. Thus, we may combine the FD and motion vector as the feature vector for a better performance. 1382 (2) FD and motion vector. We add motion information to 1383

the feature vector for our HMM modeling. We find that the 1384 recognition rate of using training data for testing is 98.5% 1385 and the recognition rate of using testing data rises to 93.5%. 1386 This method gains 3% improvement of the recognition rate 1387 using the testing data. The reason is that adding the motion 1388 1389 vector improves the recognition rate for the 9th, 12th, 17th and 18th gestures in our vocabulary. However, for some 1390 gestures, there may be a slightly performance decrement 1391 due to the different experimental environments. 1392

Fig. 21 shows the results of the gesture recognition of the 1393 1st gesture in our vocabulary. Fig. 21(a) shows the sequence 1394 of observation symbols which is input to the hmm. Fig. 1395 1396 20(b) shows the output of the maximum likelihood of each 1397 HMM applied to the testing sequence. there are totally 20 HMMS in the recognition system of which first HMM 1398 generate the largest maximum likelihood. In our exper-1399 iments, we have tested 20 different gestures from different 1400

signers, some gestures are not precise, and the recognition 1407 rate drops to 85% (see Table 3). We find that our recognition 1408 system is size and rotation insensitive, for small objects and 1409 for large objects, it can still effectively identify the correct 1410 gesture. We also find that when the symbol sequence has an 1411 error at frame 30 (symbol 35 is obtained instead of symbol 1412 21), and the score of the HMM modeling gesture 10 is very 1413 close to the score of the HMM modeling gesture 13. Our 1414 system can still recognize the gesture correctly. However, if 1415 in the beginning, the system makes many error observations 1416 and generates wrong symbols, then the HMM models will 1417 not justify the correct recognition. Another reason for error 1418 recognition is that we don't have enough training data to 1419 make a good estimate of the HMM model parameters. 1420

6. Conclusions

1425 We have developed a method to recognize the unknown 1426 input gestures by using HMMs. Since the variation of the 1427 hand gestures is usually large, the transition between states 1428 is necessary in each gesture for an effective hand tracking. 1429 We apply this system to recognize the single gesture. In the 1430 experiments, we assume stationary background so that our 1431 system will have smaller search region for tracking. With a 1432 larger training set and context modeling, lower error rates 1433 are expected and generalization to user independent gesture 1434 recognition system should be developable. Once we add a 1435 new gesture into the system, we only need to re-train 1436 another HMM for the new gesture, since the relationships 1437 between new model and the original models are 1438 independent. 1439

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